

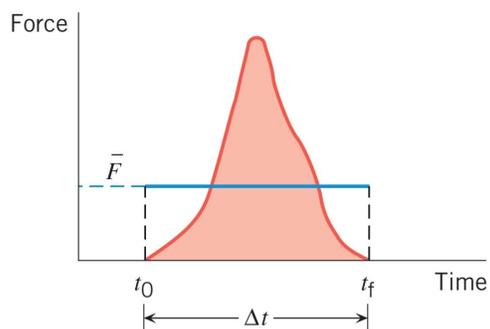
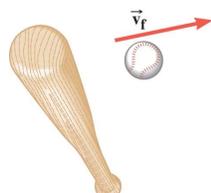
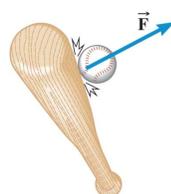
Chapter 7

Impulse and Momentum

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem



(b)

There are many situations when the force on an object is not constant.

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem

DEFINITION OF IMPULSE

The impulse of a force is the product of the average force and the time interval during which the force acts:

$$\vec{\mathbf{J}} = \vec{\mathbf{F}}\Delta t$$

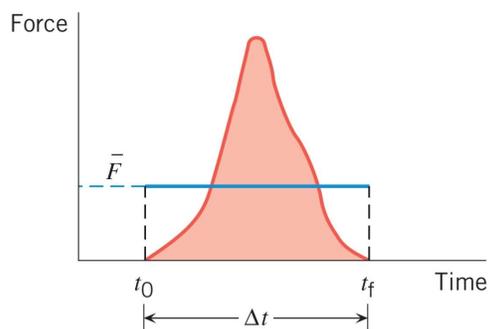
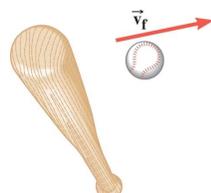
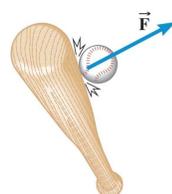
Impulse is a vector quantity and has the same direction as the average force.

newton · seconds (N · s)

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem



(b)

$$\vec{\mathbf{J}} = \vec{\mathbf{F}}\Delta t$$

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem

DEFINITION OF LINEAR MOMENTUM

The linear momentum of an object is the product of the object's mass times its velocity:

$$\vec{p} = m\vec{v}$$

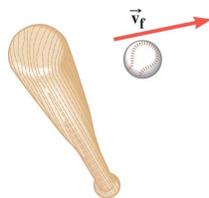
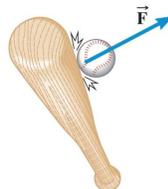
Linear momentum is a vector quantity and has the same direction as the velocity.

kilogram · meter/second (kg · m/s)

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem



$$\vec{a} = \frac{\vec{v}_f - \vec{v}_o}{\Delta t}$$

$$\sum \vec{F} = m\vec{a}$$

$$\sum \vec{F} = \frac{m\vec{v}_f - m\vec{v}_o}{\Delta t}$$

$$\left(\sum \vec{F}\right)\Delta t = m\vec{v}_f - m\vec{v}_o$$

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem

IMPULSE-MOMENTUM THEOREM

When a net force acts on an object, the impulse of this force is equal to the change in the momentum of the object

impulse

$$\left(\sum \vec{F}\right)\Delta t = m\vec{v}_f - m\vec{v}_o$$

final momentum initial momentum

WILEY

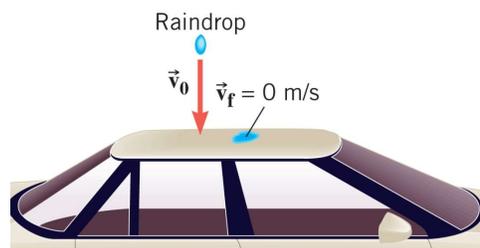
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem

Example 2 A Rain Storm

Rain comes down with a velocity of -15 m/s and hits the roof of a car. The mass of rain per second that strikes the roof of the car is 0.060 kg/s. Assuming that rain comes to rest upon striking the car, find the average force exerted by the rain on the roof.

$$\left(\sum \vec{F}\right)\Delta t = m\vec{v}_f - m\vec{v}_o$$

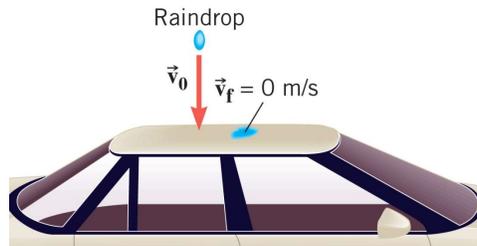


WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem

Neglecting the weight of the raindrops, the net force on a raindrop is simply the force on the raindrop due to the roof.



$$\vec{F} \Delta t = m \vec{v}_f - m \vec{v}_o \quad \longrightarrow \quad \vec{F} = - \left(\frac{m}{\Delta t} \right) \vec{v}_o$$

$$\vec{F} = -(0.060 \text{ kg/s})(-15 \text{ m/s}) = +0.90 \text{ N}$$

WILEY

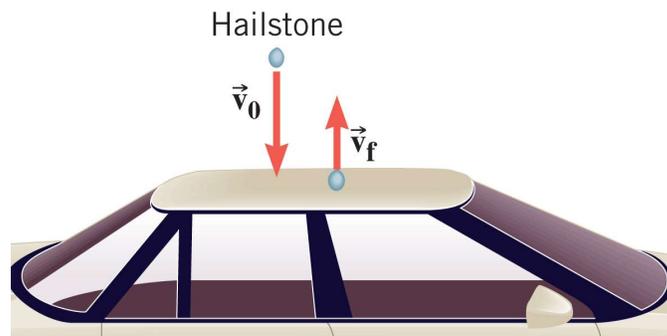
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.1 The Impulse-Momentum Theorem

Conceptual Example 3 Hailstones Versus Raindrops

Instead of rain, suppose hail is falling. Unlike rain, hail usually bounces off the roof of the car.

If hail fell instead of rain, would the force be smaller than, equal to, or greater than that calculated in Example 2?



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

WORK-ENERGY THEOREM \Leftrightarrow CONSERVATION OF ENERGY

IMPULSE-MOMENTUM THEOREM \Leftrightarrow ???

Apply the impulse-momentum theorem to the midair collision between two objects.....

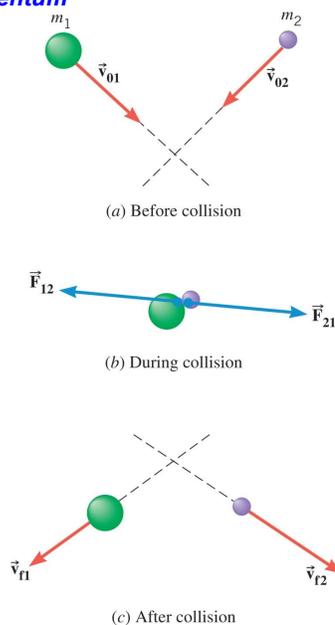
WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

Internal forces – Forces that objects within the system exert on each other.

External forces – Forces exerted on objects by agents external to the system.



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

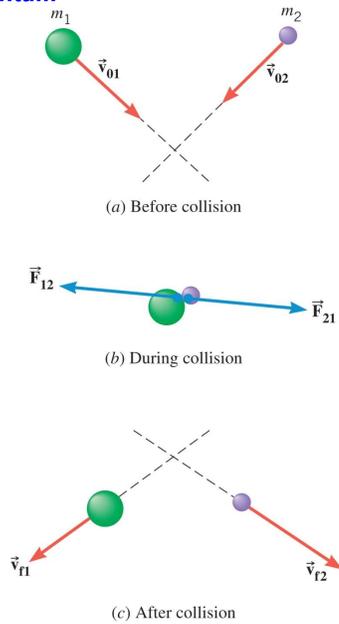
$$\left(\sum \vec{F}\right)\Delta t = m\vec{v}_f - m\vec{v}_o$$

OBJECT 1

$$\left(\vec{W}_1 + \vec{F}_{12}\right)\Delta t = m_1\vec{v}_{f1} - m_1\vec{v}_{o1}$$

OBJECT 2

$$\left(\vec{W}_2 + \vec{F}_{21}\right)\Delta t = m_2\vec{v}_{f2} - m_2\vec{v}_{o2}$$



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

$$\left(\vec{W}_1 + \vec{F}_{12}\right)\Delta t = m_1\vec{v}_{f1} - m_1\vec{v}_{o1}$$

+

$$\left(\vec{W}_2 + \vec{F}_{21}\right)\Delta t = m_2\vec{v}_{f2} - m_2\vec{v}_{o2}$$



$$\left(\vec{W}_1 + \vec{W}_2 + \vec{F}_{12} + \vec{F}_{21}\right)\Delta t = (m_1\vec{v}_{f1} + m_2\vec{v}_{f2}) - (m_1\vec{v}_{o1} + m_2\vec{v}_{o2})$$

$$\vec{F}_{12} = -\vec{F}_{21}$$

$$\vec{P}_f$$

$$\vec{P}_o$$

WILEY

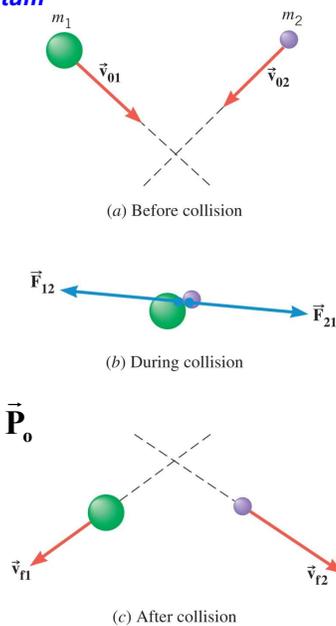
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

The internal forces cancel out.

$$(\vec{W}_1 + \vec{W}_2)\Delta t = \vec{P}_f - \vec{P}_o$$

$$(\text{sum of average external forces})\Delta t = \vec{P}_f - \vec{P}_o$$



WILEY
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

$$(\text{sum of average external forces})\Delta t = \vec{P}_f - \vec{P}_o$$

If the sum of the external forces is zero, then

$$0 = \vec{P}_f - \vec{P}_o \implies \vec{P}_f = \vec{P}_o$$

PRINCIPLE OF CONSERVATION OF LINEAR MOMENTUM

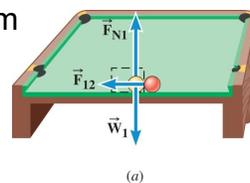
The total linear momentum of an isolated system is constant (conserved). An isolated system is one for which the sum of the average external forces acting on the system is zero.

WILEY
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

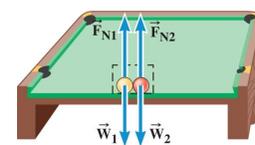
7.2 The Principle of Conservation of Linear Momentum

Conceptual Example 4 Is the Total Momentum Conserved?

Imagine two balls colliding on a billiard table that is friction-free. Use the momentum conservation principle in answering the following questions. (a) Is the total momentum of the two-ball system the same before and after the collision? (b) Answer part (a) for a system that contains only one of the two colliding balls.



(a)



(b)

WILEY

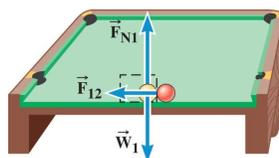
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

PRINCIPLE OF CONSERVATION OF LINEAR MOMENTUM

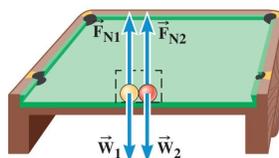
The total linear momentum of an isolated system is constant (conserved). An isolated system is one for which the sum of the average external forces acting on the system is zero.

In the top picture the net external force on the system is zero.



(a)

In the bottom picture the net external force on the system is not zero.



(b)

WILEY

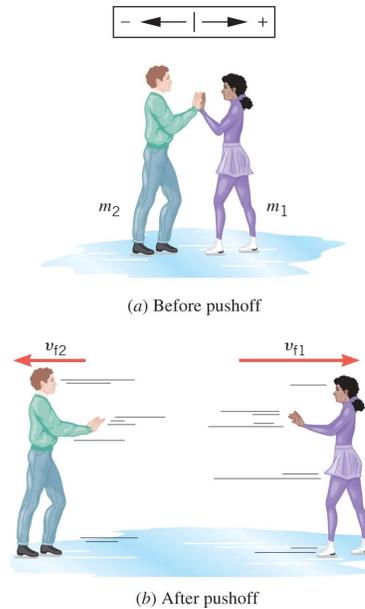
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

Example 6 Ice Skaters

Starting from rest, two skaters push off against each other on ice where friction is negligible.

One is a 54-kg woman and one is a 88-kg man. The woman moves away with a speed of +2.5 m/s. Find the recoil velocity of the man.



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

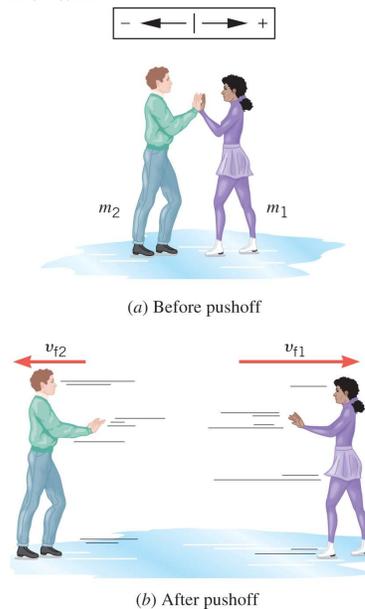
7.2 The Principle of Conservation of Linear Momentum

$$\vec{P}_f = \vec{P}_o$$

$$m_1 v_{f1} + m_2 v_{f2} = 0$$

$$v_{f2} = -\frac{m_1 v_{f1}}{m_2}$$

$$v_{f2} = -\frac{(54 \text{ kg})(+2.5 \text{ m/s})}{88 \text{ kg}} = -1.5 \text{ m/s}$$



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.2 The Principle of Conservation of Linear Momentum

Applying the Principle of Conservation of Linear Momentum

1. Decide which objects are included in the system.
2. Relative to the system, identify the internal and external forces.
3. Verify that the system is isolated.
4. Set the final momentum of the system equal to its initial momentum. Remember that momentum is a vector.

WILEY

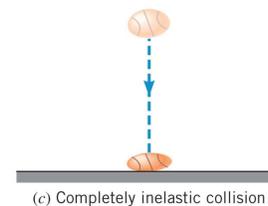
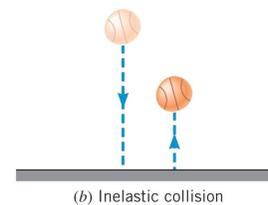
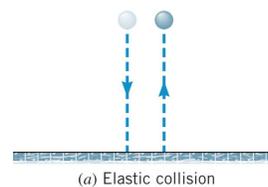
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.3 Collisions in One Dimension

The total linear momentum is conserved when two objects collide, provided they constitute an isolated system.

Elastic collision -- One in which the total kinetic energy of the system after the collision is equal to the total kinetic energy before the collision.

Inelastic collision -- One in which the total kinetic energy of the system after the collision is *not* equal to the total kinetic energy before the collision; if the objects stick together after colliding, the collision is said to be completely inelastic.



WILEY

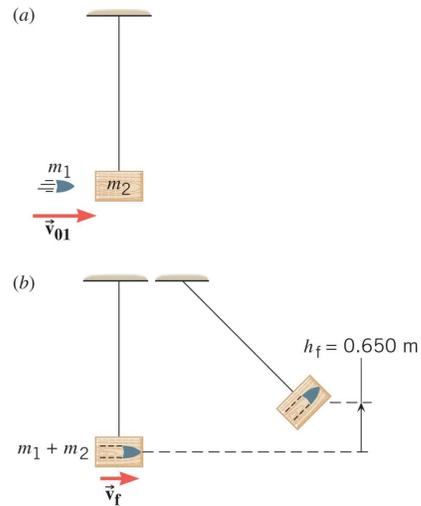
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.3 Collisions in One Dimension

Example 8 A Ballistic Pendulum

The mass of the block of wood is 2.50-kg and the mass of the bullet is 0.0100-kg. The block swings to a maximum height of 0.650 m above the initial position.

Find the initial speed of the bullet.



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

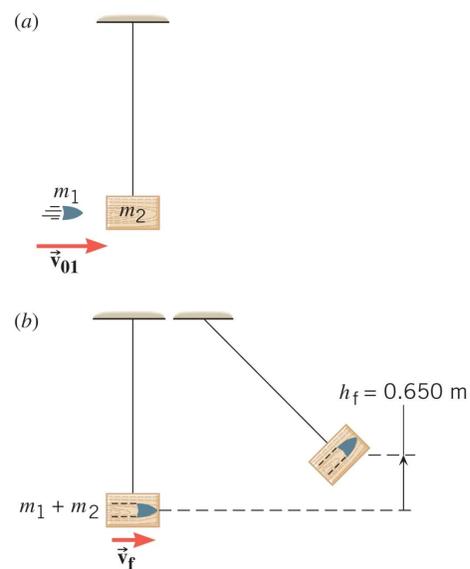
7.3 Collisions in One Dimension

Apply conservation of momentum to the collision:

$$m_1 v_{f1} + m_2 v_{f2} = m_1 v_{o1} + m_2 v_{o2}$$

$$(m_1 + m_2) v_f = m_1 v_{o1}$$

$$v_{o1} = \frac{(m_1 + m_2) v_f}{m_1}$$



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.3 Collisions in One Dimension

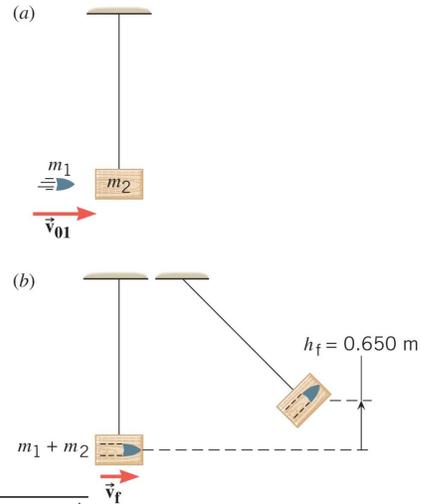
Applying conservation of energy to the swinging motion:

$$mgh = \frac{1}{2}mv^2$$

$$(m_1 + m_2)gh_f = \frac{1}{2}(m_1 + m_2)v_f^2$$

$$gh_f = \frac{1}{2}v_f^2$$

$$v_f = \sqrt{2gh_f} = \sqrt{2(9.80 \text{ m/s}^2)(0.650 \text{ m})}$$



WILEY

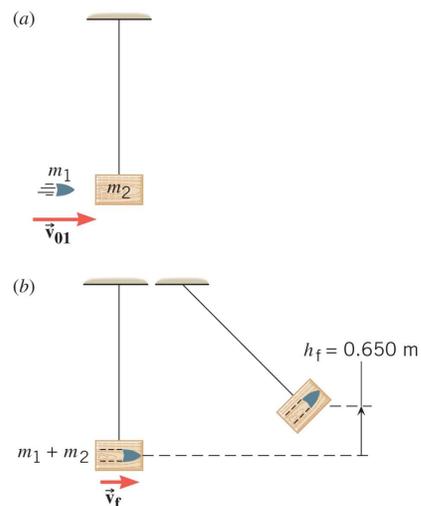
Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.3 Collisions in One Dimension

$$v_f = \sqrt{2(9.80 \text{ m/s}^2)(0.650 \text{ m})}$$

$$v_{01} = \frac{(m_1 + m_2)v_f}{m_1}$$

$$v_{01} = \left(\frac{0.0100 \text{ kg} + 2.50 \text{ kg}}{0.0100 \text{ kg}} \right) \sqrt{2(9.80 \text{ m/s}^2)(0.650 \text{ m})} = +896 \text{ m/s}$$



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.4 Collisions in Two Dimensions

A Collision in Two Dimensions

$v_{01} = 0.900 \text{ m/s}$
 $m_1 = 0.150 \text{ kg}$

$v_{02} = 0.540 \text{ m/s}$
 $m_2 = 0.260 \text{ kg}$

v_{f1}
 θ
 $v_{f2} = 0.700 \text{ m/s}$
 35.0°
 50.0°

(a)

v_{f1y}
 v_{f1x}
 θ
 v_{f1}

(b)

WILEY
 Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.4 Collisions in Two Dimensions

$$m_1 v_{f1x} + m_2 v_{f2x} = m_1 v_{o1x} + m_2 v_{o2x}$$

$$m_1 v_{f1y} + m_2 v_{f2y} = m_1 v_{o1y} + m_2 v_{o2y}$$

$v_{01} = 0.900 \text{ m/s}$
 $m_1 = 0.150 \text{ kg}$

$v_{02} = 0.540 \text{ m/s}$
 $m_2 = 0.260 \text{ kg}$

v_{f1}
 θ
 $v_{f2} = 0.700 \text{ m/s}$
 35.0°
 50.0°

(a)

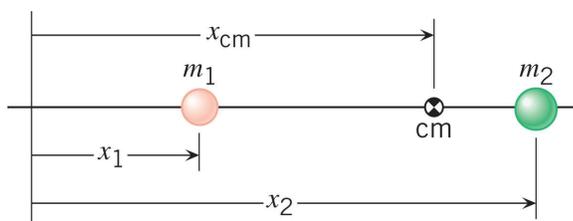
v_{f1y}
 v_{f1x}
 θ
 v_{f1}

(b)

WILEY
 Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.5 Center of Mass

The center of mass is a point that represents the average location for the total mass of a system.

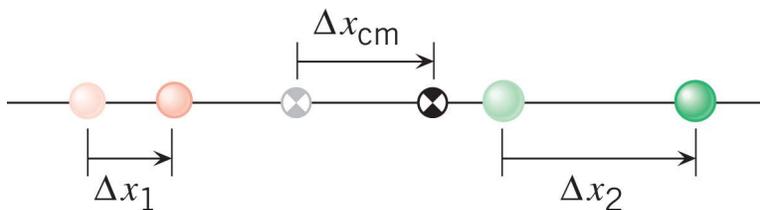


$$x_{cm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2}$$

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.5 Center of Mass



$$\Delta x_{cm} = \frac{m_1 \Delta x_1 + m_2 \Delta x_2}{m_1 + m_2} \quad \Rightarrow \quad v_{cm} = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$$

WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.5 Center of Mass

$$v_{cm} = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2}$$

In an isolated system, the total linear momentum does not change, therefore the velocity of the center of mass does not change.

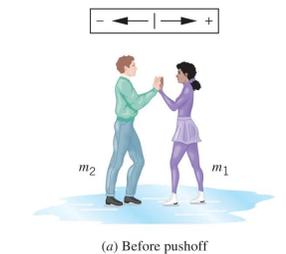
WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.

7.5 Center of Mass

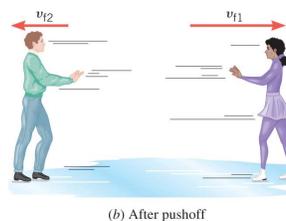
BEFORE

$$v_{cm} = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2} = 0$$



AFTER

$$v_{cm} = \frac{(88 \text{ kg})(-1.5 \text{ m/s}) + (54 \text{ kg})(+2.5 \text{ m/s})}{88 \text{ kg} + 54 \text{ kg}} = 0.002 \approx 0$$



WILEY

Copyright © 2015 John Wiley & Sons, Inc. All rights reserved.