

# Technology: Graph Systems of Inequalities

**Objective** To use a handheld to graph a system of linear inequalities

► You can use a graph to solve a system of linear inequalities.

Use a handheld to graph the system: 
$$\begin{cases} x + y < 9 \\ 2x + y \geq 14 \end{cases}$$

First, solve each inequality for  $y$ .

$$x + y < 9$$

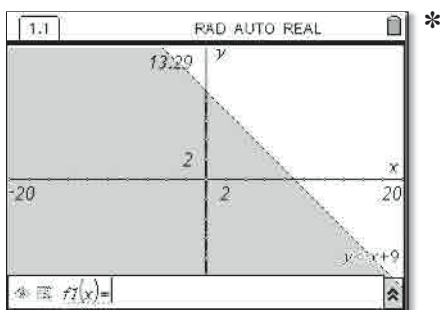
$$y < -x + 9 \quad \leftarrow \text{Use the Subtraction Property of Inequality.}$$

$$2x + y \geq 14$$

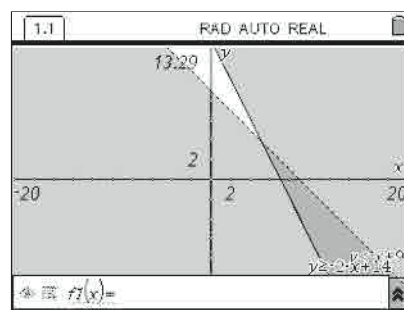
$$y \geq -2x + 14 \quad \leftarrow \text{Use the Subtraction Property of Inequality.}$$

**Step 1** Press . Then choose to select **Graphs & Geometry**.

**Step 2** Use the key to delete the equals sign. Input  $< -x + 9$ , then press to graph the inequality.



**Step 3** Use the key to delete the equals sign. Input  $\geq -2x + 14$ , then press to graph the inequality. Use to enter the inequality symbol.

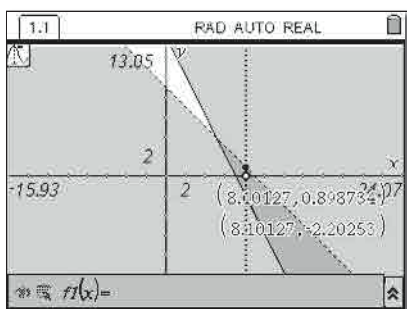


The solution to the system of inequalities is the shaded region where the two graphs overlap.

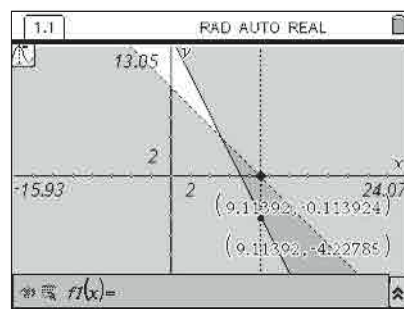
► You can use the **Trace** command to name two points that are part of a system's solution set.

**Step 4** Press menu. Select **Trace**, and then choose **Graph Trace**.

**Step 5** Press to select both lines. Then press to move along the lines. Choose a test point that is part of the solution set.  $(8, 0)$  is one point.



**Step 6** Continue to press to choose another test point. The point  $(9, -1)$  is also in the solution set.



So two points that *appear* to be part of the solution are  $(8, 0)$  and  $(9, -1)$ .

- Since you cannot verify a solution set to a system using a graph, you can use the chosen test points to check the solution algebraically.

Try: (8, 0)

$$\begin{array}{rcl} x + y < 9 & 2x + y \geq 14 \\ 8 + 0 < 9 & 2(8) + 0 \geq 14 \\ 8 < 9 \checkmark & 16 \geq 14 \checkmark \end{array}$$

Try: (9, -1)

$$\begin{array}{rcl} x + y < 9 & 2x + y \geq 14 \\ 9 + (-1) < 9 & 2(9) + (-1) \geq 14 \\ 8 < 9 \checkmark & 17 \geq 14 \checkmark \end{array}$$

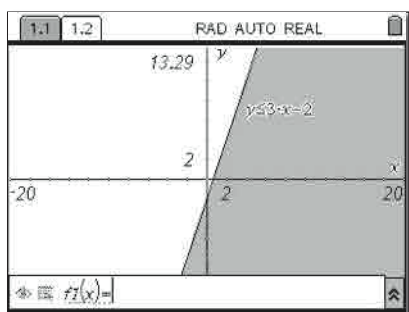
So (8, 0) and (9, -1) are part of the solution set for the inequality.

## Example

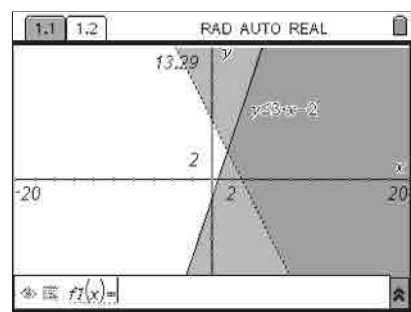
- 1** Use a handheld to graph the system.  $\begin{cases} y \leq 3x - 2 \\ y > -2x + 6 \end{cases}$

**Step 1** Press . Then choose **2** to select **Graphs & Geometry**.

**Step 2** Use the key to delete the equals sign. Input  $\leq 3x - 2$ . Use to enter the inequality symbol. Press to graph the first inequality.



**Step 3** Use the key to delete the equals sign. Input  $> -2x + 6$ , then press to graph the second inequality.



Looking at the graph, the points (5, 0) and (6, 0) *appear* to be part of the solution set. Choose test points and check the solution set.

Try: (5, 0)

$$\begin{array}{rcl} y \leq 3x - 2 & y > -2x + 6 \\ 0 \leq 3(5) - 2 & 0 > -2(5) + 6 \\ 0 \leq 13 \checkmark & 0 > -4 \checkmark \end{array}$$

Try: (6, 0)

$$\begin{array}{rcl} y \leq 3x - 2 & y > -2x + 6 \\ 0 \leq 3(6) - 2 & 0 > -2(6) + 6 \\ 0 \leq 16 \checkmark & 0 > -6 \checkmark \end{array}$$

## Try These

Use a handheld to graph the system. Then name two points that are part of the solution set.

1.  $\begin{cases} y > 5x \\ y \geq 5x - 4 \end{cases}$

2.  $\begin{cases} -4x + y > 8 \\ x + 4y > 8 \end{cases}$

3.  $\begin{cases} x - 3y < 15 \\ -6x - 8y \leq -12 \end{cases}$

4. **Discuss and Write** Graph the system  $\begin{cases} y \geq 5x + 3 \\ y < 5x - 4 \end{cases}$  using a handheld. Describe and explain the result.